

***Mathematica* Package for Posets  
And Investigation of the  
Littlewood-Richardson  
Poset Conjecture**

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With a  
**Supplement For**  
**Hook Length Poset Computations**  
By Cheryl A. Gann and Robert A. Proctor,  
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Approved by:

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# ***Mathematica* Package for Posets And Investigation of the Littlewood-Richardson Poset Conjecture**

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